

## Measurement-Based Sensitivity Estimation for Online Power System Monitoring and Control

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# Outline

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Introduction

Measurement-Based Sensitivity Computation Approach

Using Measurement-Based Sensitivities to Improve Online Tools

Concluding Remarks

# Motivation

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- ▶ The primary goal of power system operators is to **economically maintain operational reliability**
- ▶ A system is said to be **operationally reliable** if it can tolerate a limited number of equipment outages without jeopardizing continued operation
  - ▶ e.g., a system that meets the  **$N-1$  reliability criterion** can tolerate the outage of any single piece of equipment
- ▶ **Real-time operational reliability assessment (ORA)** is the main toolset used by system operators to meet their goal

## Operational Reliability Assessment (ORA)

**System  
Monitoring**

**Contingency  
Analysis**

**Security-Constrained  
Economic Dispatch  
(SCED)**

# ORA Shortcomings Contribute to Blackouts

- ▶ “With an operational state estimator and **real-time contingency analysis**, MISO operators ... [could have taken] timely actions to return the system to within limits.” -NERC, 2004
- ▶ “The system was not being operated in a secure N-1 state. This failure stemmed primarily from **weaknesses in ... operations planning and real-time situational awareness.**” -NERC, 2012

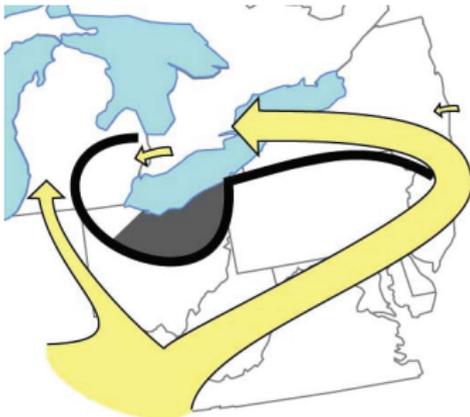


Figure: 2003 Northeast Blackout

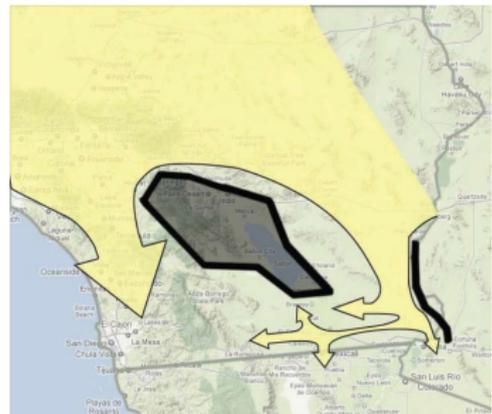
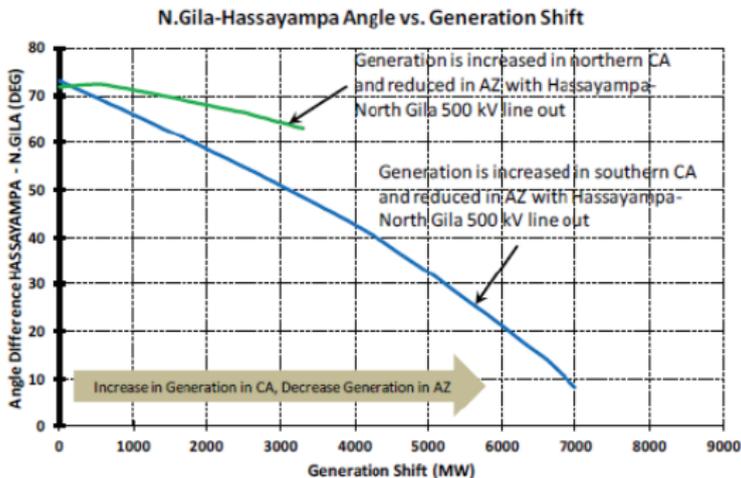


Figure: 2011 San Diego Blackout

# Conventional ORA Limitations

- ▶ “APS operators erroneously believed that they could return the line to service in approximately 15 minutes, even though they had no situational awareness of a large phase angle difference caused by the outage.”  
-NERC, 2012
- ▶ “Underlying factors that contributed to the event... [included] not providing effective tools and operating instructions for use when reclosing lines with large phase angle differences across the reclosing breakers.”  
-NERC, 2012



# Overall Project Objective

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- ▶ Linear sensitivities, e.g., Injection Shift Factors, Loss Factors, are used in many online ORA tools
- ▶ Existing approaches to computing such sensitivities typically employ an AC or DC **model**; this is not ideal because
  1. Accurate model containing up-to-date topology is required
  2. Results may not be applicable if actual system evolution does not match predicted operating points
- ▶ Phasor Measurement Units (PMUs) provide high-speed voltage and current measurements that are time-synchronized
- ▶ **Objectives:**
  1. Estimate linear sensitivities by exploiting measurements obtained from PMUs without the use of a power flow model
  2. Utilize measurement-based sensitivities to improve the performance of ORA tools

# Looking Back

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- ▶ Developed measurement-based estimation methods for
  - ▶ Power flow Jacobian [TSG '16]
  - ▶ Injection shift factors [NAPS '14, TSG '16]
  - ▶ Line outage angle factors [NAPS '15]
  - ▶ Loss factors
  
- ▶ Demonstrated key advantages of proposed measurement-based methods:
  - ▶ Eliminate reliance on system models and corresponding accuracy
  - ▶ Resilient to undetected system topology, incorrect model data, and operating point changes
  
- ▶ Demonstrated effectiveness of proposed methods for improving the performance of online tools for monitoring and control:
  - ▶ Security-constrained economic dispatch [GM '15, TPWRS '16]
  - ▶ Locational marginal price formation [TPWRS '16]

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# Power System Sensitivities

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## Fundamental sensitivities:

- ▶ Power flow Jacobian (J)
- ▶ Injection shift factors (ISFs)
- ▶ Participation factors (PFs)

## Derived sensitivities:

- ▶ Power transfer distribution factors (PTDFs)
- ▶ Line outage distribution factors (LODFs)
- ▶ Outage transfer distribution factors (OTDFs)
- ▶ Loss factors (LFs)
- ▶ Line outage angle factors (LOAFs)

# PMU-Based Sensitivity Estimation

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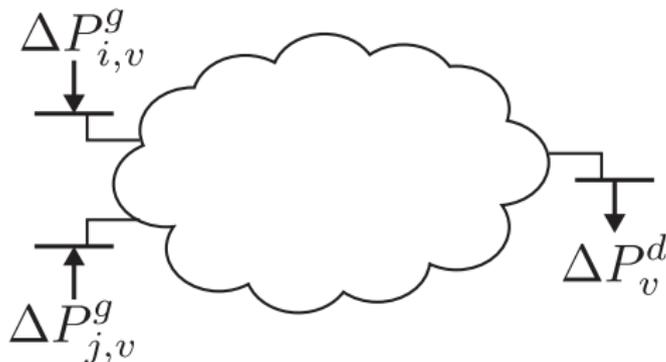
- ▶ Proposed measurement-based approach relies on **inherent fluctuations in net injections**
- ▶ Collect PMU measurements of, e.g., active flows and injections
- ▶ Cast estimation of **fundamental sensitivities** as an overdetermined linear relationship between measured quantities
- ▶ Overdetermined linear system can be solved using, e.g., least-squares error estimation (LSE)
- ▶ Other assumptions:
  - ▶ Sensitivities are approximately constant across the measurements used in the estimation
  - ▶ The regressor matrix has full column rank
- ▶ **Derived sensitivities** can be computed from fundamental ones

## Participation Factor Definition

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- ▶ The **Participation factors (PFs)** provide the sensitivity of the generator outputs to load net active power injections
- ▶ For a generator  $i$  and load  $v$ , the PF is given by:

$$\Upsilon^p[v, i] = \frac{\text{change in generator } i \text{ output}}{\text{change in load } v \text{ demand}} \approx \frac{\Delta P_{i,v}^g}{\Delta P_v^d}$$



- ▶ PFs are typically selected **on the basis of generator physical characteristics**, e.g., generator capacity or inertia constant

# PF Estimation Approach

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- ▶ We use the PFs and  $M > 2D$  load and generation measurements to form an overdetermined linear system:

$$\Delta P_i^g \approx [\Delta P^d \ \Delta Q^d] [(\Upsilon_i^p)^T \ (\Upsilon_i^q)^T]^T$$

- ▶ Overdetermined linear system can be solved with various approaches, e.g., least-squares error estimation (LSE)
- ▶ Proposed measurement-based approach relies on **inherent fluctuations in load and generation**
- ▶ Other assumptions:
  - ▶ The PFs are approximately constant across the  $M$  measurements
  - ▶ The regressor matrix  $[\Delta P^d \ \Delta Q^d]$  has full column rank

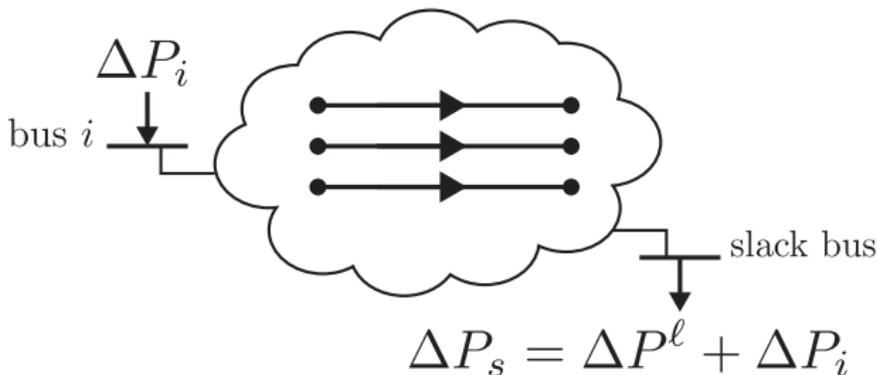
# Loss Factor Definition

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- ▶ **Loss factors (LFs)** provide the sensitivity of the system-wide losses to bus net active power injections
- ▶ For a bus  $n$ , the LF is given by:

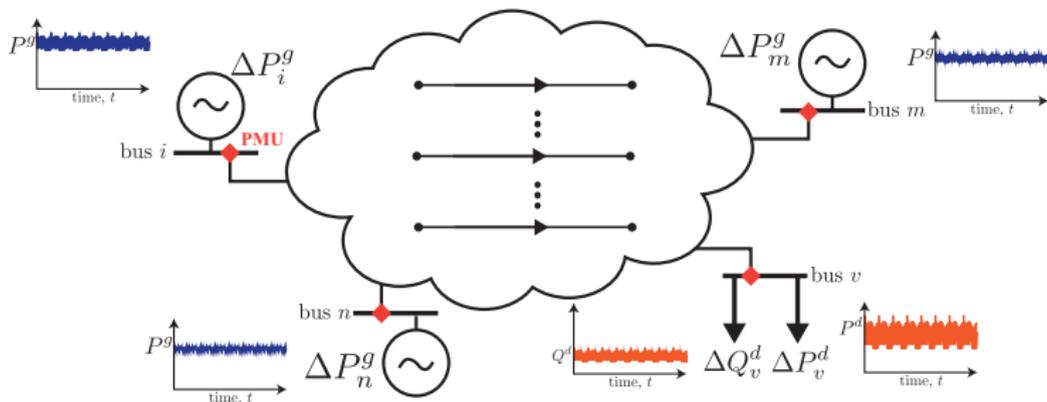
$$\Lambda_n = \frac{\text{change in system-wide losses}}{\text{change in injection at bus } n} \approx \frac{\Delta P^\ell}{\Delta P_n}$$

assuming the injection is **balanced by the slack bus**



- ▶ LFs are typically computed using a **power flow model**, a given operating point, and a **distributed slack policy**

# Measuring Loss Variation



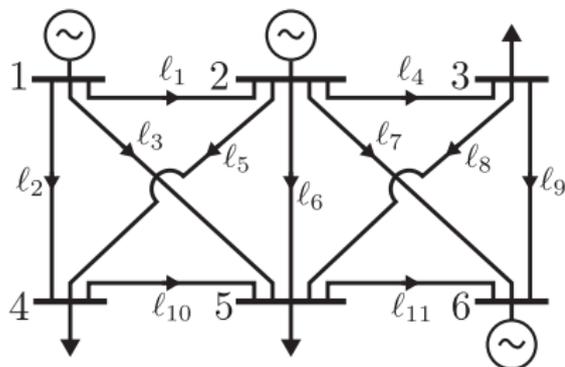
$$\Delta P_i^g[k] = P_i^g[(k+1)\Delta t] - P_i^g[k\Delta t] \quad \Delta P_v^d[k] = P_v^d[(k+1)\Delta t] - P_v^d[k\Delta t]$$

$$\Delta Q_v^d[k] = Q_v^d[(k+1)\Delta t] - Q_v^d[k\Delta t]$$

- Losses manifest as difference between load injection changes and corresponding generator output changes:

$$\Delta P^\ell[k] = \sum_{i=1}^G \Delta P_i^g[k] - \sum_{v=1}^D \Delta P_v^d[k] \quad \implies \Lambda_v \approx 1 - \sum_{i=1}^G \Upsilon^p[v, i]$$

# LF Estimation Example



- ▶ Simulate 300 measurement instances
- ▶  $P_3^d$  increased by 0.2 p.u. between instances 100 and 200
- ▶ LFs estimate computed at each measurement instance via LSE with  $M = 60$

Table: LFs at instances 75 and 225 (pre- and post-load-change)

bus	LF error					
	actual LFs		model-based		measurement-based	
	pre-change	post-change	pre-change	post-change	pre-change	post-change
1	0.0402	0.0481	-0.00179	-0.00973	0.0015	0.0020
2	0.0404	0.0426	-0.00258	-0.00473	0.0014	0.0014
3	0.0110	0.0047	-0.00243	0.00378	0.0004	0.0002
4	-0.0000	0.0045	0.00108	-0.00348	0.0003	-0.0000
5	-0.0093	-0.0078	-0.00155	-0.00303	0.0006	-0.0006
6	0.0333	0.0308	0.00329	0.00587	0.0013	0.0010
MSE:	-	-	0.0055	0.0137	0.0025	0.0028

[all values in MWh/MWh]

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# Online Tools Relying on Linear Sensitivities

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- ▶ Contingency analysis
- ▶ Generation re-dispatch
- ▶ Congestion relief
- ▶ Real-time security-constrained economic dispatch (SCED)

# Security-Constrained Economic Dispatch

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## SCED problem formulation:

$\max$  {social surplus}

( $\min$  {generator costs})

subject to:

{ power balance  $\rightarrow$  requires LFs  
equipment limits  
network flow constraints  $\rightarrow$  requires ISFs  
reliability constraints  $\rightarrow$  requires ISFs, LODFs and LOAFs

## Objective:

- ▶ Solve the SCED problem using measurement-based sensitivities in place of model based sensitivities

# Measurement-Based LMPs

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- ▶ LMPs and dispatch targets determined with the measurement-based SCED are:
  - ▶ adaptive to changing system conditions
  - ▶ not affected by erroneous data in the system model
- ▶ Measurement-based LMPs:

$$\lambda = \lambda^r \mathbf{1}_N + \begin{bmatrix} \Psi \\ \Psi^s \end{bmatrix}^T \left( \begin{bmatrix} \bar{\mu}^f \\ \bar{\mu}^s \end{bmatrix} - \begin{bmatrix} \underline{\mu}^f \\ \underline{\mu}^s \end{bmatrix} \right) + \lambda^r \Lambda$$

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$\Psi$	Injection shift factors (ISFs)
$\Psi^s$	Line flow to bus injection sensitivities for selected generator and line outages
$\Lambda$	Loss factors (LFs)
$\lambda^r$	Lagrange multiplier for power balance constraint
$\bar{\mu}^f, \underline{\mu}^f$	Lagrange multipliers for network flow constraints
$\bar{\mu}^s, \underline{\mu}^s$	Lagrange multipliers for reliability constraints

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# Case Study

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- ▶ IEEE 118-bus system with synthetic PMU measurements
- ▶ Compare SCED outcomes obtained with:
  - (i) nonlinear power flow model LFs [actual]
  - (ii) model-based LFs
  - (iii) measurement-based LFs
- ▶ **Scenario 1:** Undetected outage LF and SCED impacts
  - ▶ Undetected outage of double circuit  $\ell_{141}, \ell_{142}$
  - ▶ No binding network constraints
- ▶ **Scenario 2:** Incorrect line impedance data contingency analysis and SCED impacts
  - ▶ Scale line impedance on each of top 30% of loaded lines by  $\kappa \in [0.7, 1.3]$  drawn from a uniform distribution
  - ▶ Lower transmission limits so as to introduce congestion

# Impact on Dispatch Targets

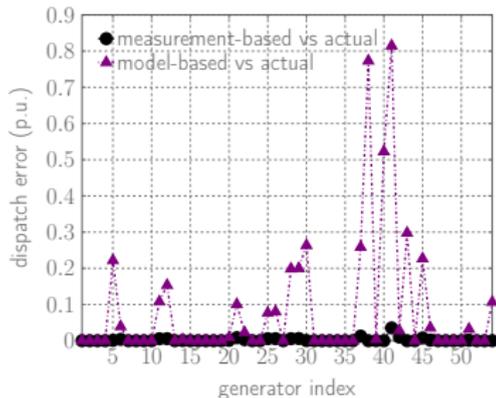


Figure: Errors in  $P_i^g$  with respect to ED solution with full power flow LFs for **Scenario 1**

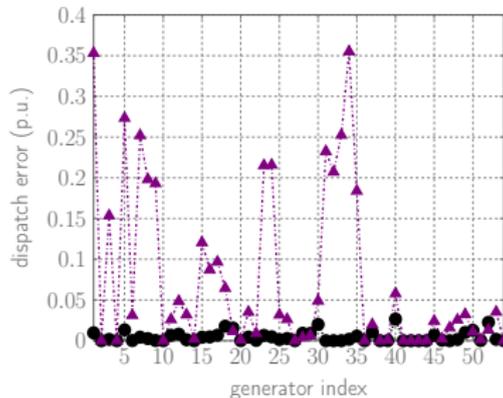


Figure: Errors in  $P_i^g$  with respect to ED solution with full power flow LFs for **Scenario 2**

# Impact on LMPs

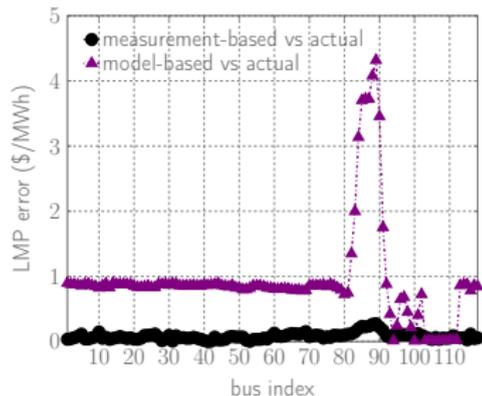


Figure: Errors in prices with respect to ED solution with full power flow LFs for **Scenario 1**

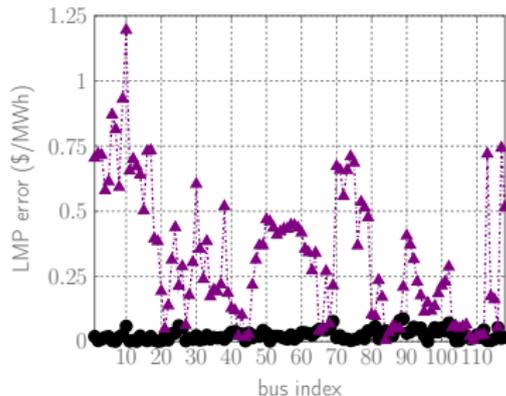


Figure: Errors in prices with respect to ED solution with full power flow LFs for **Scenario 2**

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# Contributions

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## Developed measurement-based approach for estimating sensitivities

- ▶ Utilize PMU measurements to estimate fundamental sensitivities in real-time
- ▶ Eliminates the model-dependence of the loss representation in the SCED

## Developed measurement-based SCED

- ▶ Leverage measurement-based sensitivities, e.g., LFs, to perform contingency selection and to reformulate relevant SCED constraints
- ▶ Can be executed without state-estimation or topology processing